

# STUDY OF THE UNSTEADY TRANSONIC FLOW <br> ON ROTOR BLADE WITH OIFFERENT TIP SHAPES 

BY<br>A. DESOPPER<br>ONERA<br>92320 Chatillon, FRANCE

## TENTH EUROPEAN ROTORCRAFT FORUM

AUGUST 28 - 31, 1984 - THE HAGUE, THE NETHERLANDS

# STUDY OF THE UNSTEADY TRANSONIC FLOW <br> ON ROTOR BLADE WITH DIFFERENT TIP SHAPES 

## A. DESOPPER <br> ONERA

92320 Châtillon, FRANCE

## SUMMARY

An unsteady transonic small perturbations method is used to characterize the flow on an helicopter blade in the advancing blade side where unsteady transonic flows occur. Non lifting and lifting unsteady calculation results are presented for different tip shapes.

Non lifting calculation results show the influence of sweep (backward and forward), progressive sweep with taper and anhedral effect on the intensity of the transonic flows.

The lifting calculations concern high advance ratio configurations ( $\mu>0.3$ ). They are performed on an isolated blade with an angle of attack prescribed along the blade for each azimuthal location. Three blade tips are considered : a rectangular blade and two swept tips. For the three tips the resulting computations compare well with experimental results obtained on a model rotor equiped with absolute pressure tranducers. Experimental and calculated results indicate clearly that the improvement of the performances obtained with the model rotor equiped with the swept tips compared to the ones of the same rotor equiped with rectangular blades, is mainly due to the decrease of the transonic flow intensity observed on the swept tips.

All the results obtained are very encouraging and give a certain confidence in the use of such a method as an help to design efficient tip shapes for fast forward flight.

LIST OF SYMBOLS

```
\(\mathcal{E}=\frac{1}{A R}=\frac{C}{R}=1 /(\) aspect ratio \()\)
\(c=\) chord
Cp \(=\) pressure coefficient
\(C p^{\mathbf{N}}=\) critical pressure coefficient
\(\mathrm{Ct}=\) thrust coefficient \(\quad \mathrm{Cq}=\) power coefficient
\(M=\) Mach number
M \(\omega r=\frac{\omega R}{a_{\infty}}=\) tip Mach number
\(\mathrm{R}=\) blade radius
\(r=\) radial station
\(t=\psi-90^{\circ}=\) time
Vo = forward velocity
```

```
\alpha = total angle of attack
\alpha
\mp@subsup{\alpha}{2}{}}=\mathrm{ angle of attack due to flapping
\mp@subsup{\alpha}{3}{}}=\mathrm{ angle of attack due to induced velocity
    \delta}=\mathrm{ thickness ratio
    \mp@subsup{0}{c}{}}=\mathrm{ collective pitch angle
\mp@subsup{0}{w}{}}=\mathrm{ twist angle
    \mu}=\frac{\mp@subsup{V}{0}{}}{wR}=\mathrm{ advance ratio
\sigma = solidity
\phi = velocity potential
\psi = azimuthal angle
\omega = ~ a n g u l a r ~ s p e e d
```


## 1 - INTRODUCTION -

A full calculation of the flow on an helicopter blade would require a threedimensional unsteady method able of computing various flow conditions, like :

- transonic flows for the advancing blade side,
- flows with large viscous effects for the dynamic stall problem on the retreating blade side,
- development and influence of a very complicated wake system generated by the blades.

Up to now, no practical method exists for such difficult conditions and the studies are generally limited to one aspect of this problem.

At the Aerodynamic Department of ONERA, experimental and theoretical studies of the unsteady transonic flows on the advancing blade side have been performed for about ten years now. The main purpose of these studies is to define some blade tip shapes which improve the aerodynamic and acoustic performances of a rotor by reducing the wave drag and the intensity of the transonic flows that appear on a rectangular blade for fast forward flight speed.

An unsteady transonic small perturbation method is used to computa the unsteady transonic flow of the advancing blade side. Non-lifting and lifting unsteady calculations are presented for different tip shapes.

The non-lifting calculation results show the influence of sweep (backward and forward), progressive sweep with taper and anhedral effect on the intensity of the transonic flows.

The lifting calculations are performed on an isolated blade with an angle of attack prescribed along the blade for each azimuthal location. These calculations concern high advance ratio configurations ( $\mu>0.3$ ) and three blade tip shapes are considered : a rectangular blade and two progressive swept tips. The results are compared with experimental ones obtained on a model rotor equiped with absolute pressure transducers.

The intent of this paper is to show some interesting features of the unsteady transonic flows that occur in the advancing blade side for fast forward flight speed.

## 2.1 - Non-líting calculation -

ONERA and US Army RTL at Ames have worked jointly within the framework of an M.O.U. on helicopter aeroelasticity to develop a computer program to solve the low frequency transonie small disturbance equation for rotor blades of nearly arbitrary planform [1-2] .

This equation has the form :
(1)

$$
A \frac{\partial^{2} \phi}{\partial r \partial x}=\frac{\partial}{\partial x}\left[B \frac{\partial \phi}{\partial x}+B^{\prime}\left(\frac{\partial \phi}{\partial x}\right)^{2}\right]+C \frac{\partial^{2} \phi}{\partial x \partial y}+D \frac{\partial^{2} \phi}{\partial y^{2}}+E \frac{\partial^{2} \phi}{\partial z^{2}}
$$

with

$$
\begin{aligned}
& A=2 M_{\omega R}^{2} \frac{\varepsilon}{\delta^{2 / 3}}(y+\mu \cos t) \\
& B=\frac{1-M_{\omega R}^{2}(y+\mu \cos t)^{2}}{\delta^{2 / 3}} \\
& C=2 M_{\omega R}^{2} \frac{\varepsilon}{\delta^{2 / 3}} \mu \sin t(y+\mu \cos t) \\
& D=\frac{\varepsilon^{2}}{\delta^{2 / 3}} \\
& E=1 .
\end{aligned}
$$

In order to take into account a blade tip of nearly arbitrary shape a transformation of coordinates is made. This transformation has the general form :

$$
\left\{\begin{array}{l}
\xi=\xi(x, y) \\
\eta=\eta(y) \\
\xi=\xi(z)
\end{array}\right.
$$

In this coordinates system the blade leading and trailing edges are aligned with coordinated lines $\xi=$ cst.

Deralls of the method, results and comparisons with experimental data can be found in [1 to 4]. Very good comparisons with experimental pressure measurements were obtained for a straight tip blade [3] ; however for a swept tip a too rapid disappearance of the shock wave in the second quadrant $\left(\Psi>90^{\circ}\right)$ was predicted by the calculation [3] .

Equation (1) has been obtained in considering the transonic flow condition near the azimuth $\Psi=90^{\circ}$ for which the incident Mach number is maximum. A new approach has been studied in order to extend the domain of validity of the method for a larger azimuthal sector around $\Psi=90^{\circ}$. This approach is similar to the one used at RAE for the development of a quasi-steady calculation method for transonic flows on helicopter blade [5] . In coordinates along (s) and normal ( $n$ ) to the local velocity vector the transonic small disturbances equation writes :

$$
\begin{aligned}
& M_{\omega R}^{2} \varepsilon^{2} \varnothing_{t t}+2 M_{\omega R}^{2} \varepsilon \phi_{\Delta t} \sqrt{u_{1}^{2}+u_{2}^{2}}= \\
& \varnothing_{\Delta \Delta}\left\{1-M_{\omega R}^{2}\left(u_{1}^{2}+u_{2}^{2}\right)-M_{\omega R}^{2}(\gamma+1) \phi_{\Delta} \sqrt{u_{1}^{2}+u_{2}^{2}}\right\} \\
& +\phi_{n \pi}+\phi_{33}+M_{\omega R}^{2} \varepsilon \phi_{\Delta} \frac{1}{\sqrt{u_{1}^{2}+u_{2}^{2}}}\left(-u_{2} \mu \cos t+u_{1} \mu \sin t\right) \\
& 8-5
\end{aligned}
$$

In a blade attached Cartesian coordinate system, this equation becomes :
$M_{\omega R}^{2} \varepsilon^{2} \phi_{t t}+2 M_{\omega R}^{2} \frac{\varepsilon}{\delta^{2 / 3}} u_{1} \varnothing_{x t}-2 M_{\omega R}^{2} \frac{\varepsilon^{2}}{\delta^{2 / 3}} u_{2} \phi_{y t}$
$\frac{1}{\left(u_{1}^{2}+u_{2}^{2}\right)}\left(u_{1}^{2} \phi_{x x}+u_{2}^{2} \varepsilon^{2} \phi_{y y}-2 u_{1} u_{2} \varepsilon \phi_{x y}\right)$

$$
\left\{\frac{1-M^{2} \omega_{R}\left(u_{1}^{2}+u_{2}^{2}\right)}{\delta^{2 / 3}}-M_{\omega_{R}}^{2}(\gamma+1)\left(u_{1} \varnothing_{x}-\varepsilon u_{2} \varnothing_{y}\right)\right\}
$$

(1')

$$
\begin{aligned}
& +\frac{u_{2}^{2}}{\left(u_{1}^{2}+u_{2}^{2}\right)} \frac{\varnothing_{x x}}{\delta^{2 / 3}} \\
& +\frac{u_{1}^{2}}{\left(u_{1}^{2}+u_{2}^{2}\right)} \frac{\varepsilon^{2}}{\delta^{2 / 3}} \emptyset_{y y} \\
& +\frac{2 u_{1} u_{2}}{\left(u_{1}^{2}+u_{2}^{2}\right)} \frac{\varepsilon}{\delta^{2 / 3}} \varnothing_{x y} \\
& +\emptyset_{33} \\
& +\frac{\varepsilon}{\delta^{2 / 3}} M_{\omega R}^{2}\left(\mu \sin t+u_{2}\right) \varnothing_{x}+\frac{\varepsilon^{2} M_{\omega R}^{2}}{\delta^{2 / 3}}\left(u_{1}+\mu \cos t\right) \varnothing_{y} \\
& \left\{\begin{array}{l}
u_{1}=y+\mu \cos t \\
u_{2}=\varepsilon x+\mu \sin t
\end{array}\right.
\end{aligned}
$$

with

In this equation no hypothesis is made concerning the spanwise flow ( $u_{2}$ ) relative to the chordwise one ( $u_{1}$ ). For $\psi=90^{\circ}\left(t=0 ., u_{2} \simeq 0\right.$.) and $M_{\omega R}^{2} \mathcal{E}^{2} \varnothing_{\text {tt }} \quad$ negleted (low reduced frequency) the equation (1') is quite close to equation (1).

The $\varnothing_{y} t$ term and the modification of the transonic term (underlined) have been taken into account in a simplified way. In the coordinates system $\xi, \eta, \zeta$ linked to the shape of the blade only the derivative terms in $\xi$ like $\frac{\partial \phi}{\partial \xi}$ and $\frac{\partial^{2} \varnothing}{\partial \xi^{2}}$ have been kept for these two terms.
The surface tangency condition has been modified from: $\phi_{3}=(y+\mu \cos t) f^{\prime} x(x, y)$ to $\phi_{3}=(y+\mu \cos t) f^{\prime} x(x, y)-\mu \sin t \mathcal{C}^{\prime} y(x, y)$ , where $f(x, y)$ represents the equation of the upper, or lower surface of the blade.

These modifications have improved the results obtained for non-rectangular blade with a better prediction of the phase shift of the transonic flows on a $30^{\circ}$ sweptback tip (Fig. 1) and a disappearance of the shock wave after $\psi=90^{\circ}$ in good agreement with the experimental one. A better stability of the method has also been obtained and for all the calculations presented in this paper a time step of at least $\Delta \psi=1^{\circ}$ has been used.

## 2.2 - Lifting calculation -

For lifting calculations the influence of the complex wake system has to be taken into account. As the calculations concern high advance-ratio flight configurations ( $\mu>0.3$ ), where the induced downwash is small, an angle-of-attack approach has been adopted.

The unsteady lifting calculations are performed on an isolated blade with an angle of attack prescribed along the blade for each azimuthal location by

$$
\alpha(r / R, \Psi)=\theta_{c}+\theta_{w}(r / R-0.7)+\alpha_{1}+\alpha_{2}+\alpha_{3}
$$

The experimental values are used for the rotor shaft angle, the collective pitch angle, the blade twist argle and the flapping angle. The induced incidence ( $\alpha_{3}$ ) has been calculated using the simple DREES downwash model [6]. More details concerning this angle-of-attack approach and some results can be found in [7].

For the boundary condition on the wake, the spanwise velocity component is now taken into account. This gives an oblique wake for the azimuts different of $90^{\circ}$.

3 - NON-LIFTING UNSTEADY CALCULATION RESULTS -
Different tip shapes have been studied (Fig. 2) :

- rectangular,
. swept back tip of $30^{\circ}$ between. .9R and $R$ (F30)
. swept forward tip of $30^{\circ}$ between. 9R and $R \quad(F-30)$,
- progressive swept tip with taper (PF2),
- rectangular with an anhedral tip of $10^{\circ}$ between .9R to $R$.

The calculations results presented Fig. 3 to 11 correspond to the following conditions : advance ratio $\mu=0.5, M_{\omega R}=.64$, blade with a profile of constant thickness $\delta=11 \%$., low aspect ratio $=7$.

The supersonic flows occuring on the blades are characterized by the evolution of the maximum local Mach number and the one of the extent of supercritical flows.

## 3.1 - Comparison between rectanqular, F30, F-30 blade tips : (Figs. 3-4)

The evolutions of the maximum local Mach number versus span location are compared for the rectangular blade, F30 and F-30 at different azimuths (Fig. 3).

Compared to the rectangular blade :

- at $\psi=60^{\circ}$, the intensity of the transonic flows decreases for the sweptback tip on the last $15 \%$ of the blade (between . 85 R and R ) ; on the swept forward tip an higher Mach number is observed at the beginning of the swept tip (.9R),
- at $\Psi=90^{\circ}$ a slight expansion can be noticed on the constant sweptback tip.
- after $\psi=90^{\circ}$ this expansion on $F 30$ increases and spreads along the blade.

The evolution of the maximum local Mach number with the azimuthal location and the one of the extent of supercritical flows show a phase shift of the supersonic flows with sweep :

- on the sweptback tip, the supercritical flows appear later in azimuth (compared to the straight tip) with a decrease of their intensity before $\psi=90^{\circ}$, and disappear later after $90^{\circ}$ with an increasing expansion at the tip,
- on the swept forward tip an opposite effect can be observed ; the supercritical flows appear sooner in azimuth before $90^{\circ}$ and disappear sooner after $90^{\circ}$.


## 3.2 - Comparison between rectangular, F30, PF2 blade tips - (Figs. 5-6)

The leading edge line of the PF2 tip has a parabolic shape between. 95 R and R and the sweep angle of the leading edge is $80^{\circ}$ at the tip. A more precise definition of this PF2 tip defined at ONERA can be found in [9]. The intensity of the transonic flows is smaller on this PF2 tip compared to the straight one for almost all the advancing blade side. In particular the expansion seen on F30 is strongly reduced and at $\psi=90^{\circ}$ the maximum local Mach numbers are the smallest for the last $20 \%$ of the blade span for this PF2 tip. However for $130^{\circ}<\psi$ the transonic flows are slightly stronger on the PF2 tip than on the straight tip.

The isomach-1ines at $\Psi=60,90$ and $120^{\circ}$ (Figs. 7-8-9) give an overall view of the flows on the four different blade tips. The intensity of the transonic flows is strongly reduced on the PF2 tip where a weak shock becomes visible only at $\psi=120^{\circ}$.
3.3 - Unsteady esóect ó an anhedral tip - (Figs. 10-11)

The blade considered is a rectangular one with an anhedral tip of $10^{\circ}$ between $.9 R$ and $R$.

The pressure distributions at the radial station .95R (Fig. 10) and the lift coefficient azimuthal evolutions at. .91 R and .95 R show that the effects of the anhedral tip are :

- to give a positive lift before $90^{\circ}$ and a negative lift after $90^{\circ}$ as it was expected,
- to increase the transonic flows on the upper surface before $90^{\circ}$ and to decrease them after $90^{\circ}$.

This effect can be combined with planform shapes one to reduce the intensity of the transonic flows on the upper surface of a blade for forward flight at high advance ratio.

These "non-lifting" calculations show that an optimized blade tip shape for the whole advancing blade side is not easy to define. A constant swept tip weakens the shock intensity around the azimuth $\psi=90^{\circ}$. As the incident Mach number is maximum for this azimuth such effect should improve the aerodynamic performances of a rotor by decreasing the drag and have favorable effect on the acoustic characteristics by lessening what acousticians call delocalization. However a part of this improvement can be lost by stronger shock in another azimuthal sector, for example in the second quadrant for a constant swepback tip. One possible solution is to take a progressive swept tip like the PF2 one with large sweep angle at the tip in order to extend the azimuthal sector where the shocks are weakened. An other possibility could be to combine sweep and anhedral geometry.

Experimental results obtained with a lifting model rotor [8] as well as flight test results [9.] have confirmed the improvements expected with new tip shapes like the PF2 one. The lifting calculations presented below show that it becomes possible to predict the unsteady flows on such tip shapes for the advancing blade side.

4 - LIFTING UNSTEADY CALCULATION RESULTS -
The method described in [7] and 2.2 has been used to perform unsteady lifting calculations for three blade tips :

- rectangular one as a reference,
- an RAE swept tip designed by the Royal Aircraft Establisment [8] , - a FL5 swept tip designed by ONERA.

The results are compared with experimental ones obtained on a model rotor equiped with absolute pressure transducers at radial stations . 85 R , . 9 R and .95R. The tests were performed in $S 2$ Chalais Meudon wind-tunnel with a twisted 3-bladed rotor.

## 4.1 - Comparisons between experimental and calculated results bor the straight tip.

Some results concerning the configurations $\frac{C_{T}}{\sigma}=0.05$, Vo $=76 \mathrm{~m} / \mathrm{s}$ and $\frac{C_{T}}{\sigma}=0.0665$, $V 0=81 \mathrm{~m} / \mathrm{s}$ have already been published in [7].

Results obtained for a more loaded case $\left(\frac{C_{T}}{\sigma}=0.075\right)$ at higher forward speed (Vo $=91 \mathrm{~m} / \mathrm{s}$ ) are presented on figures 12 and 13 . The evolution of the pressure distributions with azimuth (Fig. 12) and the pressure coefficients at different chordwise locations of the span section. 9 R are well predicted (Fig. 13). In particular the development of a strong shock on the upper surface of the blade between $\psi=80^{\circ}$ and $\Psi=160^{\circ}$.

The comparisons presented on figures 14 to 16 show that the calculation is able to predict the evolution of the transonic flows on the blade for conditions of loads and forward speeds more and more severe. A shock wave is still visible at the azimuth $\psi=150^{\circ}$ for the configuration $\frac{C_{T}}{\sigma} \overline{\bar{C}}_{T} 0.075$, Vo $=91 \mathrm{~m} / \mathrm{s}$ whereas the flow is only slightly transonic for the case $\frac{C_{T}}{\sigma}=0.05$, Vo $=76 \mathrm{~m} / \mathrm{s}$.

In general the calculation gives a shock wave with a slightly stronger intensity and located more downstream than in the experiment. This can be due to the simple inflow model used but more likely to the lack of any viscous effect in the calculations. This has been shown in 2D unsteady calculations [10] and the results obtained by $3 D$ quasi- steady calculation with and without boundary layer corrections show the same tendancy (Fig. 17 ).

## 4.2 - Comparisons between experimental and calculated results bor the RAE tip -

The RAE progressive swept tip designed by the Royal Aircraft Establishment ( Fig .18 ) has a leading edge sweep angle of the order of $75^{\circ}$ at the tip. The results presented on figure 19 concern the configuration $\frac{C_{T}}{\sigma}=.0665$, $V o \simeq 82 \mathrm{~m} / \mathrm{s}$. The experimental and calculated evolutions with azimuth of
the maximum local Mach number and of the extent of supercritical flow for the RAE and the straight tips illustrate the influence of a progressive sweptback tip :

- a clear decrease of the intensity of the transonic flows around $\Psi=90^{\circ}$,
. a delay in the appearance of transonic flows on the swept tip with a tendancy to maintain supercritical flows longer in the second quadrant.

The upper-surface pressure distributions at $\psi=90^{\circ}$ (Fig. 20) show that the effects of the progressive sweptback tip increase with forward speed. On the swept tip the shocks strength is still relatively weak at the forward speed of $90 \mathrm{~m} / \mathrm{s}$. More experimental results concerning this RAE tip can be found in [8].

## 4.3 - Comparisons between experimental and calculated results bor the FL5 tip -

The FL5 progressive swept tip design by ONERA (Fig. 18) has a linear evolution of the leading edge sweep angle between $R-1.05 \mathrm{c}$ and $\mathrm{R}-0.52 \mathrm{c}$ and an another one between $R-0.52 c$ and $R$ with $a$ value of $72.5^{\circ}$ at the tip.

Pressure distributions for sections .9R (Fig. 21) and .95R (Fig. 22) at different azimuths show good agreement between experimental results and calculated ones. The evolutions of the pressure coefficient at different chordwise locations of the section .95 R are relatively smooth without sharp discontinuities that the motion of a strong shock would give. This was not the case for the straight tip (Fig. 13) where the result of the backward and forward motions of a strong shock wave are quite visible. However the isomach lines on the upper surface presented Fig. 24 show supercritical flow evidence up to the span section .5 R at $\psi=120^{\circ}$ and $150^{\circ}$.

In spite of transonic flows of slightly higher intensity on RAE and FLS tips (Fig. 25) after $\psi=140$ or $150^{\circ}$, the clear decrease of their intensity for $\psi<130^{\circ}$ is certainly the main reason of the improvement in the performances obtained with the model rotor equiped with the swept tips compared to the ones of the same rotor equiped with rectangular blades. At high speed and high lift an improvement of $7-8 \%$ for the power required by the rotor has been obtained with the FLS tip (Fig. 26).

These calculated results obtained for the rectangular, RAE and FLS blades are very encouraging and give a certain confidence in using such a method as an help to design efficient tip shapes for fast forward flight. However improvements of the method should be probably obtained with the use of a more sophisticated inflow model like the vortex point method developed at ONERA [ll]. All the results presented concern very stiff blade and the influence of some deformations is going to be studied for comparisons with flight test results.

5 - CONCLUSION -
An unsteady transonic small perturbations method has been used to predict the flows on an helicopter blade in the advancing blade side where unsteady transonic flows occur. Non 1 ifting and lifting calculations have been performed for different tip shapes.

The non lifting unsteady calculations concern :

- a rectangular blade,
- a swept back tip,
- a swept forward tip,
- a progressive swept tip with taper,
- a rectangular tip with an anhedral geometry.

They show that an optimized blade tip shape for the whole advancing blade side is not easy to define. A constant swept tip weakens the shock intensity around the azimuth $\psi=90^{\circ}$ but give a stronger shock in an other azimuthal sector. A progressive swept tip with large sweep angle at the tip extends the azimuthal sector (around $90^{\circ}$ ) where the shocks are weakened. Positive results could certainly be obtained by combining sweep and anhedral.

The lifting calculations concern high advance ratio configurations ( $\mu>0.3$ ). Three blade tips were considered : a rectangular and two evolutive swept tips. The resulting computations compare well with experimental results obtained on a model rotor equiped with absolute pressure transducers. The experimental and calculated results indicate clearly that the improvement of the performances, obtained with the model rotor equiped with the swept tips compared to the ones of the same rotor equiped with rectangular blades, is mainly due to the decrease of the transonic flow intensity observed on the swept tips. All these results are very encouraging and give a certain confidence in the use of such a method as an help to design efficient tip shapes for fast forward flight.

Improvements of the method should be obtained with the use of a more sophisticated inflow model than the J. DREES formulation ; in particular for lower advance ratios for which the downwash level is larger. Development of unsteady full potential or Euler equations codes would also increase the domain of validity of such method.

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Fig. $1-30^{\circ}$ swept back tip


Anhedral effect


Fig.2- Study of different tip shapes. Non lifting unsteady calculations

Fig.3-Study of different tip shapes . Non lifting unsteady calculations


$$
\mu=0.5 \quad M_{\omega R}=0.64 \quad \text { NACA } 0011
$$

Maximum local Mach number and chordwise extent of supercritical flows



Fig.5-Study of different tip shapes . Non lifting unsteady calculations


Maximum local Mach number andichordwise extent of supercritical flows

$$
\mu=0,5 \quad M \omega_{R}=0.64 \quad \text { NACA } 0011
$$

$\begin{array}{ll} & \text { Rectangular } \\ \cdots & F 30 \\ \text {-acee } & \text { PF2 }\end{array}$



Fig.6-Study of different tip shapes. Non lifting unsteady calculations


1so-Mach lines
$\mu=0.5$
$M_{\omega R}=0.64$
NACA 0011
Fig.7-Study of different tip shapes. Non lifting unsteady calculations


Fig.8- Study of different tip shapes. Non lifting unsteady calculations

Iso-Mach lines
$\mu=0.5$
$M_{\omega R}=0.64$
NACA 0011

Fig.9-Study of different tip shapes. Non lifting unsteady calculations


$$
\mu=0.5 \quad M_{\omega R}=0.64
$$

$$
\begin{aligned}
& \text { —_ Upper surface } \\
& \text { - Lower surface }
\end{aligned}
$$







Fig. 10- Unsteady calculations. Rectangular blade with anhedral tip


Fig. 11-Unsteady calcuiations. Rectangular blade with anhedral tip

$C_{T} / \sigma=0.075 \quad V_{0}=91 \mathrm{~m} / \mathrm{s} \quad \omega_{R}=210 \mathrm{~m} / \mathrm{s}$

Calculation

- Upper surface


## Experiment

$\therefore$
$\stackrel{\wedge}{\wedge}$

Fig. 12-Lifting unsteady calculation. Rectangular blacie

Fig. 13-Lifting unsteady calculation. Rectangular blacte

$$
C_{T} / 0=0.075 \quad \begin{gathered}
V_{0}=91 \mathrm{~m} / \mathrm{s} \\
\text { Upper surface } \quad / / R=0.9
\end{gathered} \omega R=210 \mathrm{~m} / \mathrm{s}
$$




Fig.14- Lifting unsteady calculation. Rectangular blade


Fig. 15- Lifting unsteady calculation. Rectangular blade


Fig. 16 - Lifting unsteady calculation. Rectangular blade


Fig. 17 - Quasi steady calculations Influence of viscous effect


Fig. 18- FL5 and RAE tips blade

$$
\begin{aligned}
& C_{T} / \sigma=0.065 \quad V_{0}=82 \mathrm{~m} / \mathrm{s} \quad \\
& \begin{array}{c}
\text { Rectangular } \\
\text { Uper surface }
\end{array} \\
& \text { RAE } \\
&
\end{aligned}
$$



Fig. 19- Lifting unsteady calculations. Rectangular and RAE blades

$$
\begin{array}{lll}
C_{T} / \sigma=0.0665 & \omega R=210 \mathrm{~m} / \mathrm{s} & \psi=90^{\circ} \\
-V_{0}=69 \mathrm{~m} / \mathrm{s} & -\quad-V_{0}=82 \mathrm{~m} / \mathrm{s} & -V_{0}=90 \mathrm{~m} / \mathrm{s}
\end{array}
$$

## Calculation




Fig.20- Lifting unsteady calculations. Rectangular and RAE blades


Fig.21-Lifting unsteady calculation. FL5 blade



$$
\begin{gathered}
C_{T} / \sigma=0.0665 \\
M_{\omega R}=0.614 \\
V_{0}=83.2 \mathrm{~m} / \mathrm{s} \\
\Gamma / R=0.95
\end{gathered}
$$

Fig.22- Lifting unsteady calculation. FL5 blade


Fig.23- Lifting unsteady calculation. FL 5 blade

## Iso-Mach lines (upper surface)



Fig.24- Lifting unsteady calculation.FL5 blade

$C_{T} / \sigma=0.0665$
$V_{0}=81.4 \mathrm{~m} / \mathrm{s}$
$\omega R=210 \mathrm{~m} / \mathrm{s}$

## Calculation

- Upper surface
--_ Lower surface
Experiment
ig.25- Lifting unsteady calculations.
Rectangular and FL5 blades


Fig.26- Power required by a rotor

