

# VIBRATION REDUCTION ANALYSES USING INDIVIDUAL BLADE PITCH CONTROLS FOR LIFT-OFFSET ROTORS

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## Abstract

This work attempts to reduce the hub vibratory loads of a lift-offset rotor using IBC (Individual Blade pitch Control) in high-speed forward flight. As a lift-offset rotor for the present study, the rigid coaxial rotor of XH-59A compound helicopter is considered, and CAMRAD II is used to predict the hub vibration and rotor performance. Using the IBC with a single harmonic input at 200 knots, the vibration index of the XH-59A rotor is minimized by about 62% when the 3/rev actuation frequency is applied with the IBC amplitude of  $1^\circ$  and control phase angle of  $270^\circ$  ( $3P/1^\circ/270^\circ$ ); however, the rotor effective lift-to-drag ratio is reduced by 3.43%. When the 2/rev actuation frequency with the amplitude of  $2^\circ$  and control phase angle of  $270^\circ$  ( $2P/2^\circ/270^\circ$ ) and the 3/rev actuation frequency using the magnitude of  $1^\circ$  and control phase angle of  $210^\circ$  ( $3P/1^\circ/210^\circ$ ) are used in combination for the IBC with multiple harmonic inputs, the vibration index is reduced by about 62%, while the rotor effective lift-to-drag ratio increases by 0.37% at a flight speed of 200 knots. This study shows that the hub vibration of the lift-offset rotor in high-speed flight can be reduced significantly but the rotor performance increases slightly, using the IBC with multiple harmonic inputs.

## 1. INTRODUCTION

Lift-offset helicopters using ABC<sup>TM</sup> (Advancing Blade Concept, [1]) have been developed to solve the low-speed flight performance of conventional helicopters. As seen in Figure 1, the lift-offset helicopter uses a counter-rotating rigid coaxial rotor. Since most lift is generated by the advancing blades, the lift-offset rotor can avoid the dynamic stall on the retreating side of a rotor and may produce more lift as compared to a conventional helicopter rotor. Therefore, the rotation speed of the lift-offset rotor can be reduced moderately, and high-speed flight is possible with help of auxiliary propulsions [2].

Although lift-offset compound helicopters have showed excellent high-speed flight performance, they have a serious vibration problem during high-speed flights. In flight tests of the XH-59A compound helicopter, significant 3/rev cockpit vibration was observed because of the use of a rigid coaxial rotor and the absence of a vibration control system [3]. To solve this vibration problem in high-speed flights, the X2 technical demonstrator and S-97 Raider apply the AVCS (Active Vibration Control System, [4]) to their airframes. The AVCS consists of accelerometers and circular force generators with electric motors and eccentric masses. The X2 technical demonstrator using the AVCS reduced the 4/rev

cockpit vibration significantly in high-speed flights [5]. The AVCS can successfully alleviate the airframe vibration of lift-offset helicopters; however, it cannot reduce the vibration of a rigid coaxial rotor, which is the main source of vibration for the lift-offset helicopter. Therefore, the high levels of rotor vibration may still lead to serious constraints such as a restricted flight envelope, low fatigue life of the structural components, and a resultant high operating cost.

There have been numerous experimental and numerical works on active rotor controls such as HHC (Higher harmonics pitch control, [6]), IBC (Individual blade pitch control, [7]), active trailing-edge flap rotor [8], and active twist rotor [9] in order to reduce the rotor vibration of conventional helicopters. These active rotor controls usually excite the fixed or rotating system of a rotor with a single higher harmonic input to modify directly the periodic aerodynamic loads acting on the rotor blades for vibration reduction. However, there is only one research using the active rotor control to reduce the vibration of the lift-offset rotor [10]. In this work [10], HHC was applied to both the upper and lower rotors to reduce the vibration of the XH-59A rotor. Although the HHC in the numerical analysis could significantly reduce the vibration of the XH-59A rotor in high-speed flights, the actuation frequency of the HHC is restricted as

the  $(N_b-1)$ ,  $N_b$ , and  $(N_b+1)/\text{rev}$  frequency. In addition, the rotor performance was not investigated when HHC was used to reduce the vibration of the XH-59A lift-offset rotor. It is known that it is not easy to obtain rotor vibration reduction and rotor performance improvement simultaneously by using active rotor control with a single harmonic input [7].

There are limited works on vibration analyses of the lift-offset rotor using rotorcraft comprehensive analyses [10-12]. The RCAS (Rotorcraft Comprehensive Analysis System, [13]) was used to investigate the performance, loads, and vibration of the XH-59A rotor in high-speed forward flight [11]. In addition, a validation study of the performance, loads, and vibration was conducted using CAMRAD II (Comprehensive Analytical Method of Rotorcraft Aerodynamics and Dynamics II, [14]) for the XH-59A rotor in hover and forward flight conditions [12]. However, there is no research using the rotorcraft comprehensive analyses for the vibration reduction of the lift-offset rotor using IBC. The IBC has an advantage that the actuation frequency is not restricted and is more appropriate for the lift-offset rotor than the active trailing-edge flap and active twist rotors since the lift-offset rotor uses rigid blades with high stiffness.

Therefore, this paper aims to reduce the vibration of the lift-offset rotor using IBC in high-speed flights. As the lift-offset rotor, the XH-59A rotor is considered and CAMRAD II is used to analyze the vibration and performance of the XH-59A rotor using IBC. When 3/rev hub vibratory loads are minimized using the IBC with a single harmonic input, a decrease in the rotor effective lift-to-drag ratio is investigated. In addition, it is shown that the vibration reduction and performance improvement of the lift-offset rotor can be simultaneously obtained when 2/rev and 3/rev actuations are applied in combination for the IBC using multiple harmonic inputs.

## 2. ANALYTICAL METHODS

### 2.1. Analytical Model

The XH-59A lift-offset rotor is used as an analysis model using IBC in this work. The XH-59A helicopter using ABC<sup>TM</sup> was initially developed as a pure helicopter configuration without auxiliary propulsions in 1964 [1]. After flight tests in pure helicopter mode were conducted successfully in 1973, two auxiliary propulsions were added to the

aircraft for transformation into a compound helicopter ([1], Figure 1). Table 1 summarizes the general properties of the XH-59A helicopter [1]. It is well known that the hub vibration characteristics of a lift-offset rotor are dependent of the cross-over angle [10]. The cross-over angle is defined as the rotor azimuth angle where the upper and lower blades of a rigid coaxial rotor cross over each other (Figure 2). When a cross-over angle of  $0^\circ$  is used for the XH-59A rotor, the 3/rev hub axial force, normal force, and pitch moment are only transmitted to the fuselage because of inter-rotor cancellation [3, 10]. In addition, the pitch inputs with higher harmonics do not alter the inter-rotor cancellation [10].

### 2.2. Analysis Tool

This work uses CAMRAD II [14], which is a comprehensive analysis code for the performance, the aerodynamic and structural loads, and the aeroelastic stability of rotorcrafts. CAMRAD II includes nonlinear finite elements, multibody dynamics, and rotorcraft aerodynamics along with various inflow or wake models. The finite elements of nonlinear elastic beam components are used for the structural dynamics modeling of isotropic or composite rotor blades. A finite beam element has a total of 15 degrees of freedom. The lifting-line theory with the unsteady aerodynamics is used to calculate the aerodynamic loads acting on the rotor blade. In addition, CAMRAD II has the prescribed wake, rolled-up wake, multiple-trailer wake, and multiple-trailer wake with consolidation. The Newton-Raphson method with a Jacobian matrix is used for trim tasks in CAMRAD II analysis. The thrust, rolling moment, and pitching moment are considered as the trim targets. The trim analysis usually uses a low azimuthal resolution of  $15^\circ$ .

### 2.3. Modeling and Analysis Techniques

The CAMRAD II model for the XH-59A rotor using IBC in the present study is based on the model constructed in the authors' previous work [12]. Therefore, most modeling and analysis techniques of the present CAMRAD II analysis are the same as those given in Ref. [12]. Figure 3 shows the CAMRAD II model for the XH-59A with the cross-over angle of  $0^\circ$  in this work. A blade of the XH-59A rotor is represented using seven nonlinear finite beam elements. The pitch hinge is located at the 5% blade radius. The rotor control system including the pitch link, swashplates, and pitch horn is also included. It is assumed that the stiffness of the pitch link with the IBC actuator is

the same as that of the original XH-59A rotor model used in the previous work [12]. In this work, the pitch motion by the IBC inputs applied to both the upper and lower rotors is represented using Eq. (1).

(1a) For a single harmonic input,

$$\theta_{IBC} = A \cos(N\psi - \phi)$$

(1b) For multiple harmonic inputs,

$$\theta_{IBC} = \sum_{N=2}^3 A_N \cos(N\psi - \phi_N)$$

where  $\theta_{IBC}$  is the IBC equivalent blade pitch,  $\psi$  is the blade azimuth angle, and  $N$ ,  $A$ , and  $\phi$  are the actuation frequency, amplitude, and control phase angle of the IBC inputs, respectively.

Since the actual airfoil data for the XH-59A rotor are not available, the airfoils similar to the actual airfoil characteristics of the XH-59A rotor are used as given in Figure 4. However, the drag increment is used appropriately in order to correct the aerodynamic characteristics of the airfoils used in the present analyses. Further detailed explanation for the adjustment of drag coefficients in the C81 airfoil tables is given in Ref. [12]. The aerodynamic loads on each blade are calculated using 16 aerodynamic panels. Unlike the authors' previous work [12], which used a general freewake model, the prescribed wake model is used in the present analyses to avoid the convergence trouble due to the application of the IBC inputs.

The trim analyses are conducted using the six primary rotor controls of the upper and lower rotors. The pitch angle of the XH-59A compound helicopter is fixed at  $0^\circ$  since it provides the best performance for the lift-offset rotor [1]. The trim targets in the validation examples in Section 3.1 are set as the vertical force equivalent to the aircraft weight, the torque offset of the upper and lower rotors, and the hub pitching and rolling moments of the upper and lower rotors. In particular, the hub rolling moments ( $M_{roll}$ ) can be prescribed using the assumed lift-offset value given Eq. (2).

$$(2) \quad LOS = \frac{M_{roll}}{TR}$$

where  $T$  is the thrust of each rotor.

For the propulsive trim, which will be used in Sections 3.2 and 3.3, the drag force of each rotor is considered as the trim target instead of the

pitching moment of each rotor. In the present analyses, the drag forces obtained from the validation examples in Section 3.1 are used as the target values of drag forces for the propulsive trim.

The 3/rev hub vibratory loads of the XH-59A rotor are calculated using Eq. (3).

$$(3) \quad (F/M)_{3P} = \sqrt{\left[ \left( \frac{F}{M} \right)_{3P_c}^{upper} + \left( \frac{F}{M} \right)_{3P_c}^{lower} \right]^2 + \left[ \left( \frac{F}{M} \right)_{3P_s}^{upper} + \left( \frac{F}{M} \right)_{3P_s}^{lower} \right]^2}$$

where  $F$  and  $M$  are the hub forces and moments, respectively. In addition, the superscripts upper and lower mean the upper and lower rotors, respectively, and the subscripts  $c$  and  $s$  represent the cosine and sine components of the hub loads, respectively.

The vibration index (VI, [15]) to evaluate the vibration level of the XH-59A rotor is defined as

$$(4) \quad VI = K_F \frac{F_{H_{3P}}}{W_0} + K_M \frac{M_{H_{3P}}}{RW_0}$$

where  $F_{H_{3P}} = \sqrt{(0.5F_{x_{3P}})^2 + (0.67F_{y_{3P}})^2 + F_{z_{3P}}^2}$  and  $M_{H_{3P}} = \sqrt{M_{x_{3P}}^2 + M_{y_{3P}}^2}$ . In addition,  $W_0$  is the aircraft weight.  $K_F$  and  $K_M$  are assumed as unity in this work. It should be noted that the inter-rotor cancellation of the lift-offset rotor [10] is considered when the vibration index is calculated.

The rotor power ( $P$ ) of each of the upper and lower rotors for performance calculation of the lift-offset rotor is defined as

$$(5) \quad P = P_i + P_o + P_p$$

where  $P_i$ ,  $P_o$ , and  $P_p$  are the induced power, profile power, and parasite power, respectively.

The rotor effective lift-to-drag ratio ( $L/D_e$ ) to evaluate the rotor performance is defined as

$$(6) \quad \frac{L}{D_e} = \frac{L}{(P_{coaxial}/V + X)}$$

where  $P_{coaxial}$  is the power of the lift-offset rotor which is the sum of each power of the upper and lower rotors. In addition,  $V$  and  $X$  are the flight speed and drag force of the lift-offset rotor, respectively.

### 3. RESULTS and DISCUSSIONS

#### 3.1. Validation

The modeling and analysis techniques of CAMRAD II using the prescribed wake model are validated for the XH-59A rotor without IBC in this section. For the analyses, the XH-59A rotor in compound helicopter mode with auxiliary propulsions (gross weight of 13,000 lb) is considered, and the lift-offset of 0.25 is used. Figure 5 shows the correlation of the rotor effective lift-to-drag ratio in forward flight between the present prediction and flight test data [16]. The flight test data in Figure 5 are for a gross weight ranging from 11,000 to 13,000 lb. As seen in the figure, the present prediction compares well with the flight test data since the CAMRAD II analysis result is within the upper and lower bounds of the flight test data, and the variation of the predicted result is similar to that of the test data. Figure 6 compares the predicted 3/rev hub pitch moment with the flight test data [1] for the XH-59A rotor with a cross-over angle of  $0^\circ$ . Although correlations between the present analysis and test data are given at only two flight speed conditions in the figure, the present CAMRAD II analysis predicts well the 3/rev hub pitch moment. As given in Figures 5 and 6, it is believed that the present modeling and analysis techniques to predict the rotor performance and vibration are well established.

#### 3.2. IBC using a single harmonic input

In this section, the 3/rev hub vibratory loads and rotor performance are investigated when the IBC with a single harmonic input (Eq. 1(a)) is used for the XH-59A rotor at a flight speed of 200 knots. For the IBC with a single harmonic input, three actuation frequencies ( $N$ ) of 2, 3, and 4/rev and two IBC amplitudes ( $A$ ) of 1 and  $2^\circ$  are used. The control phase angle ( $\phi$ ) from 0 to  $360^\circ$  is considered with an increment of  $30^\circ$ . The propulsive trim is used for the analyses with and without the IBC, as previously described.

##### 3.2.1 Rotor vibration

Figure 7 shows the change in the vibration index (Eq. (4)) of the XH-59A rotor in terms of the control phase angle. The baseline indicates the result when the IBC is not applied. As seen in the figure, the vibration index of the XH-59A rotor changes (increases or decreases) significantly when the IBC with a single harmonic input is used. The vibration index is reduced by about 59.3% from the baseline value when the actuation frequency of 2/rev, IBC amplitude of  $2^\circ$ , and control phase of  $180^\circ$  ( $2P/2^\circ/180^\circ$ ) are used for

IBC. In addition, when the IBC with  $3P/1^\circ/270^\circ$  is used, the vibration index is minimized with reduction of about 62% as compared to the baseline value. The IBC using  $4P/1^\circ/330^\circ$  also moderately reduces the vibration index by approximately 44%. However, the vibration index is reduced by about 3% only when the IBC with  $3P/2^\circ/270^\circ$  is applied. The maximum reduction in the vibration index is summarized in Figure 8 for various IBC input conditions. As shown in Figures 7 and 8, the IBC inputs using  $2P/2^\circ/180^\circ$  and  $3P/1^\circ/270^\circ$  both show excellent vibration reductions of the XH-59A rotor by about 59.3 and 62%, respectively.

Changes in the 3/rev hub load components in terms of the control phase angle are investigated in Figure 9. As given in the figures, the variation trends for two different IBC amplitudes of 1 and  $2^\circ$  are similar to each other with the given actuation frequency. The 3/rev hub axial force in Figure 9(a) is minimized by approximately 73.1% from the baseline value when the IBC using  $3P/2^\circ/120^\circ$  is applied. Figure 9(b) shows that the 3/rev hub normal force is minimized by about 83.8% when the IBC input of  $3P/1^\circ/270^\circ$  is used. The IBC using  $3P/1^\circ/240^\circ$  in Figure 9(c) minimizes the 3/rev hub pitch moment by about 65.4% to the baseline value. As shown in Figure 9, the IBC input conditions are different to minimize the 3/rev hub axial force, normal force, and pitch moment, respectively. However, all of the 3/rev hub load components are minimized by the IBC using the 3/rev actuation frequency.

Figure 10 summarizes the maximum reductions in the 3/rev hub axial force, normal force, and pitch moment for the given actuation frequency and IBC amplitude, and shows the corresponding control phase angles. Particularly the IBC using  $4P/2^\circ/330^\circ$  minimizes the 3/rev hub pitch moment, but its reduced value is higher than the baseline value by 50%. As shown in the figures, there is no control phase angle, which simultaneously minimizes the 3/rev hub axial force, normal force, and pitch moment for the given actuation frequency and IBC amplitude. Furthermore, when two IBC amplitudes of 1 and  $2^\circ$  are considered with the given actuation frequency, the control phase angle is the same to minimize the 3/rev hub load component.

As shown in Figures 7 to 10, two IBC input conditions,  $2P/2^\circ/180^\circ$  and  $3P/1^\circ/270^\circ$ , are appropriate to reduce significantly the vibration index of the XH-59A rotor at 200 knots. In addition, the control phase angle to minimize the vibration index is the same as that to minimize the 3/rev hub normal force when the actuation

frequency and IBC amplitude are given. For these two IBC input conditions, the 3/rev hub normal force is minimized the most as compared to the reductions in the other 3/rev hub load components. Therefore, the control phase angle to minimize the vibration index is also the same as the control phase angle, which provides the greatest maximum reduction in the 3/rev hub load components. However, it is known that the 3/rev pitch moment of the XH-59A rotor is the most dominant to excite the airframe in high-speed flights when a cross-over angle of  $0^\circ$  is used [1, 10].

### 3.2.2 Rotor performance

The variations of the rotor effective lift-to-drag ratio are given in Figure 11 when the IBC with a single harmonic input is used for the XH-59A rotor at 200 knots. As shown in the figure, the rotor performance increases or decreases by the IBC application. When Figures 7 and 11 are compared, it is easily known that the IBC input to minimize the vibration of the XH-59A rotor reduces the rotor performance. For an example, the IBC using  $3P/1^\circ/270^\circ$  which minimizes the vibration index by about 62%, reduces the rotor effective lift-to-drag ratio by about 3.43% as compared to the baseline performance. In other words, it is difficult to obtain the vibration reduction and performance improvement of a lift-offset rotor simultaneously when using the IBC with a single harmonic input. Figure 12 summarizes the maximum improvement of the rotor effective lift-to-drag ratio for various IBC input conditions. The IBC with  $2P/2^\circ/0^\circ$  maximizes the rotor performance of the XH-59A rotor by 3.18% to the baseline value. However, the IBC using the 4/rev actuation does not increase the rotor effective lift-to-drag ratio but decreases the rotor performance, as seen in Figures 11 and 12, although the IBC using 4/rev actuation reduces the vibration index discussed previously in Figures 7 and 8.

### 3.3. IBC using multiple harmonic inputs

As shown in the previous section, the IBC using a single harmonic input reduces significantly the vibration index of the XH-59A rotor at a flight speed of 200 knots; however, the rotor effective lift-to-drag ratio is reduced when the IBC to minimize the rotor vibration is used. Therefore, a new input scenario of IBC is required to reduce significantly the hub vibratory loads while maintaining or increasing the rotor performance of a lift-offset rotor in high-speed flights. In this section, the IBC using multiple harmonic inputs is proposed to reduce the vibration index and

increase the rotor effective lift-to-drag ratio (or at least maintain the baseline value) of the XH-59A rotor at 200 knots, simultaneously. The different actuation frequencies ( $N$ ), IBC amplitudes ( $A_N$ ), and control phase angles ( $\varphi_N$ ) are combined using Eq. 1(b) for the IBC with multiple harmonic inputs.

Two actuation frequencies of 2 and 3/rev, two IBC amplitudes of 1 and  $2^\circ$ , and control phase angles from  $0$  to  $360^\circ$  with an increment of  $30^\circ$  are combined for the IBC with multiple harmonic inputs. As previously discussed in Section 3.2, since the IBC using a 4/rev actuation does not increase the rotor performance, the 4/rev actuation is not considered for multiple harmonic inputs of the IBC. Actually, it is an optimization problem to find the conditions of multiple harmonic inputs for the IBC, which simultaneously minimizes the vibration and maximizes the performance of the lift-offset rotor in high-speed flights. However, the goal of this study is not to search for the optimal input condition for simultaneous vibration minimization and performance maximization of the XH-59A rotor. Instead, this paper shows an example using the IBC with multiple harmonic inputs, which reduces the vibration index significantly and increases slightly the rotor effective lift-to-drag ratio of the XH-59A, simultaneously. Two input conditions of  $2P/2^\circ/270^\circ$  and  $3P/1^\circ/\varphi_3$  are combined for the IBC using multiple harmonic inputs.

#### 3.3.1 Rotor vibration

Figure 13 shows the variation of the vibration index of the XH-59A rotor at 200 knots, using the IBC with the multiple harmonic inputs;  $\theta_{IBC} = 2\cos(2\psi - 270^\circ) + 1\cos(3\psi - \varphi_3)$ . As shown in the figure, the vibration index changes as the control phase angle for the 3/rev actuation ( $\varphi_3$ ) varies. The vibration index is minimized by about 62% from the baseline value when a control phase angle ( $\varphi_3$ ) of  $210^\circ$  is used for the IBC with multiple harmonic inputs. The capability of this vibration reduction is exactly equivalent to that using the IBC with the single harmonic input of  $3P/1^\circ/270^\circ$  given in Figures 7 and 8.

Figure 14 exhibits the variations of the 3/rev hub axial force, normal force, and pitch moment in terms of the control phase angle ( $\varphi_3$ ) for the IBC using multiple harmonic inputs. Although the vibration index is reduced seriously from the baseline result given in Figure 13, the 3/rev hub axial force in Figure 14(a) is not reduced as compared to the corresponding baseline value since its minimized value is higher than the baseline value by about 48.8%. The 3/rev hub normal force in Figure 14(b) is minimized by

approximately 64.5% to the baseline value when the IBC using the multiple harmonic inputs with  $\varphi_3$  of  $240^\circ$  is used. The variation of the 3/rev hub pitch moment is given in Figure 14(c). The multiple harmonic inputs using  $\varphi_3$  of  $210^\circ$  minimizes the 3/rev hub pitch moment with a reduction of about 87.6% from the baseline value. Figure 15 summarizes the maximum reduction in 3/rev hub load components and the corresponding IBC input conditions using multiple harmonic inputs. When the IBC using multiple harmonic inputs is applied, the 3/rev hub pitch moment is minimized the most as compared to the other 3/rev hub load components. As shown in Figures 14 to 15, the control phase angle for the 3/rev actuation ( $\varphi_3$ ) to minimize the vibration index is the same as the control phase angle ( $\varphi_3$ ), which gives the greatest maximum reduction in the 3/rev hub load components.

### 3.3.2 Rotor performance

Figure 16 shows the variation of the rotor effective lift-to-drag ratio in terms of the control phase angle ( $\varphi_3$ ) for the IBC using multiple harmonic inputs;  $\theta_{IBC}=2\cos(2\psi-270^\circ)+1\cos(3\psi-\varphi_3)$ . When the control phase angle ( $\varphi_3$ ) is  $150^\circ$ , the rotor performance is maximized by 3.16% as compared to the baseline value. The rotor effective lift-to-drag ratio increases by 0.37% when a control phase angle ( $\varphi_3$ ) of  $210^\circ$ , which minimizes the vibration index as given in Figure 13, is used. Therefore, the IBC using multiple harmonic inputs,  $\theta_{IBC}=2\cos(2\psi-270^\circ)+1\cos(3\psi-210^\circ)$ , significantly reduces the rotor vibration while it slightly increases the rotor performance for the XH-59A lift-offset rotor at 200 knots.

When two present prediction sets using control phase angles ( $\varphi_3$ ) of  $180^\circ$  and  $210^\circ$  are interpolated, the vibration reduction and rotor performance improvement of the XH-59A rotor can be summarized as in Table 2. As given in the table, when a control phase angle ( $\varphi_3$ ) of  $200^\circ$  is used for the present multiple harmonic inputs of IBC, the rotor vibration is reduced by about 50% from the baseline value, and the rotor performance is improved by approximately 1.01% as compared to the baseline result, simultaneously. It is not easy to obtain this outperformance in the simultaneous vibration reduction and performance improvement of the XH-59A rotor when the IBC using a single harmonic input is used.

## 4. CONCLUSIONS

In this work, the vibration and performance of the

XH-59A lift-offset rotor using IBC were investigated by the rotorcraft comprehensive analysis code, CAMRAD II. At a flight speed of 200 knots, the vibration index was reduced by about 62% from the baseline value, but the rotor effective lift-to-drag ratio was reduced by about 3.43% to the baseline result when the actuation frequency of 3/rev, IBC amplitude of  $1^\circ$ , and control phase of  $270^\circ$  ( $3P/1^\circ/270^\circ$ ) were used for the IBC with a single harmonic input. However, when the IBC with multiple harmonic inputs;  $\theta_{IBC}=2\cos(2\psi-270^\circ)+1\cos(3\psi-210^\circ)$ , was used for the XH-59A rotor at 200 knots, the rotor vibration was reduced by about 62% and the rotor performance was improved by about 0.37% from the baseline value. Using the obtained prediction results, the vibration index was reduced by approximately 50% while the rotor effective lift-to-drag ratio increased by about 1.01% when the IBC using  $\theta_{IBC}=2\cos(2\psi-270^\circ)+1\cos(3\psi-200^\circ)$  was applied to the XH-59A lift-offset rotor at 200 knots. In the future, a physical understanding of the prediction results given in this paper will be investigated thoroughly, and an optimization study of the input scenario for the IBC using multiple harmonic inputs, which minimizes the vibration reduction and maximizes the rotor performance of the lift-offset rotor simultaneously, will be conducted.

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(a) XH-59A technical demonstrator

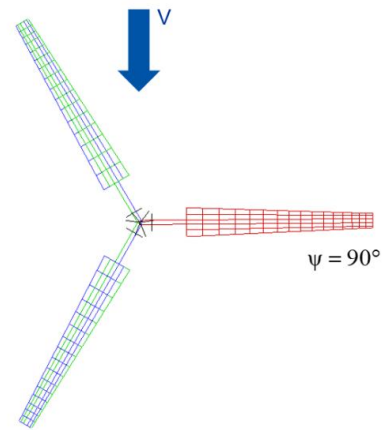
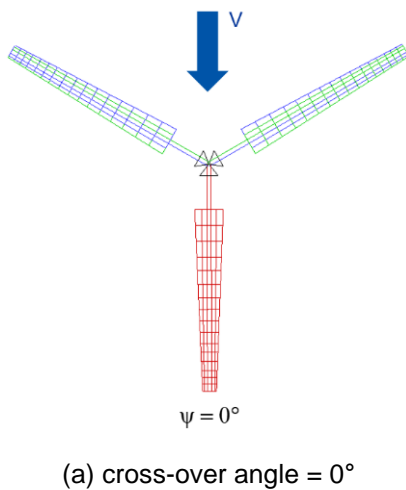


(b) X2 Technical demonstrator



(c) S-97 Raider

Figure 1. Lift-offset helicopters using ABC™.



(b) cross-over angle = 90°

Figure 2. Definition of cross-over angle.

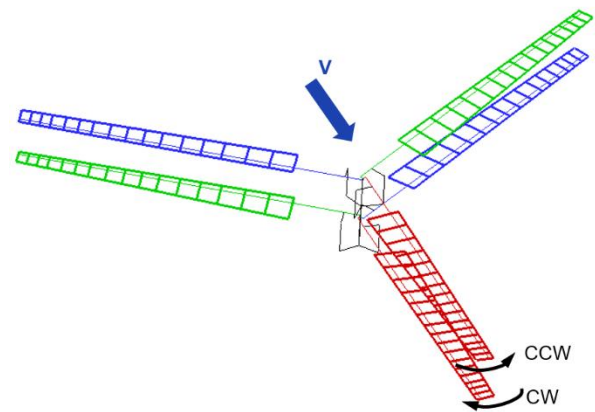
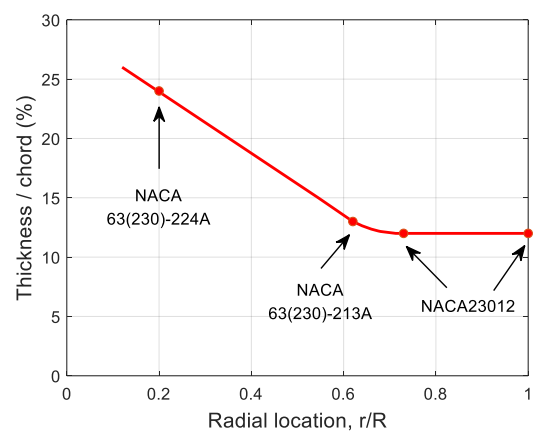
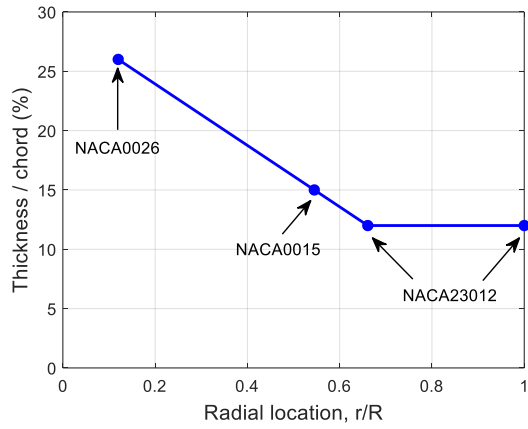


Figure 3. CAMRAD II model for XH-59A rotor.



(a) Actual airfoils





(b) Present airfoils

Figure 4. Blade thickness and airfoil distribution.

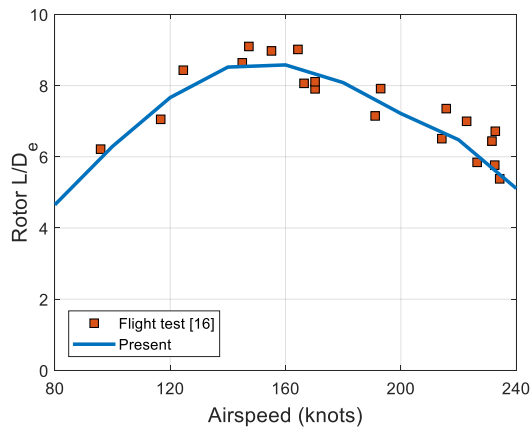


Figure 5. Validation of rotor effective lift-to-drag ratio.

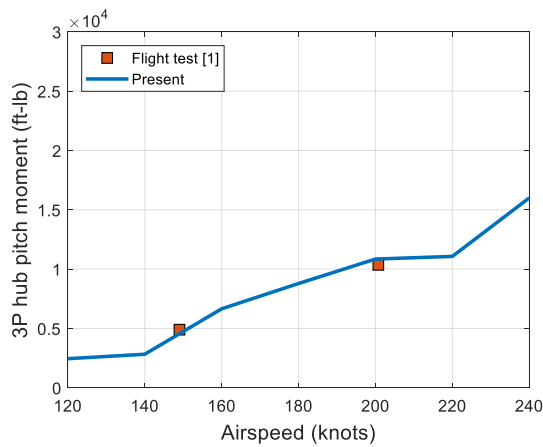


Figure 6. Validation of 3/rev hub pitch moment.

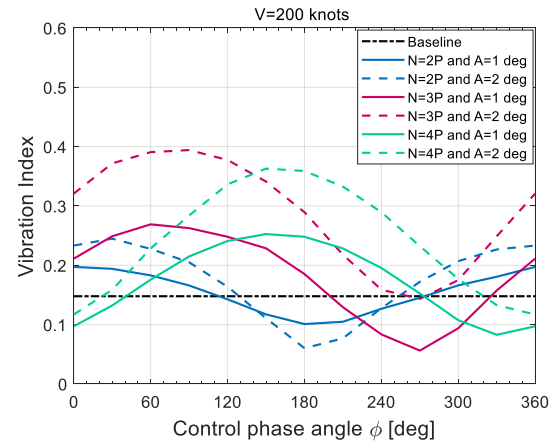


Figure 7. Vibration index in terms of control phase angle for IBC using a single harmonic input.

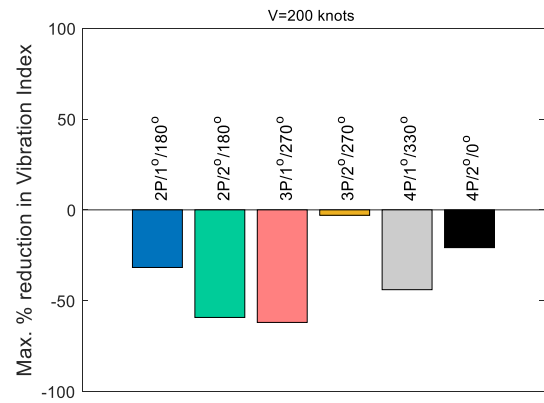
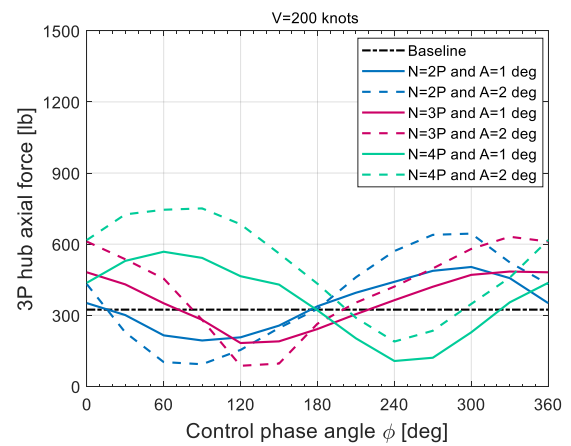
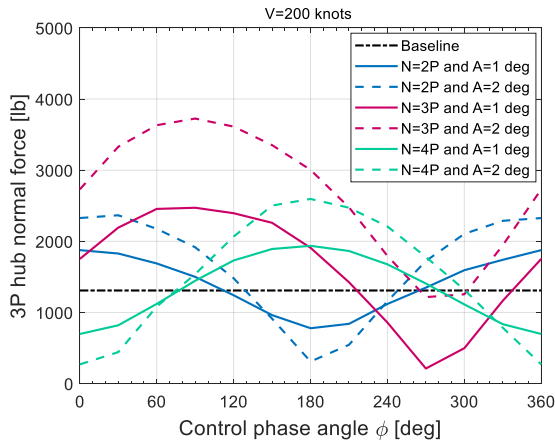


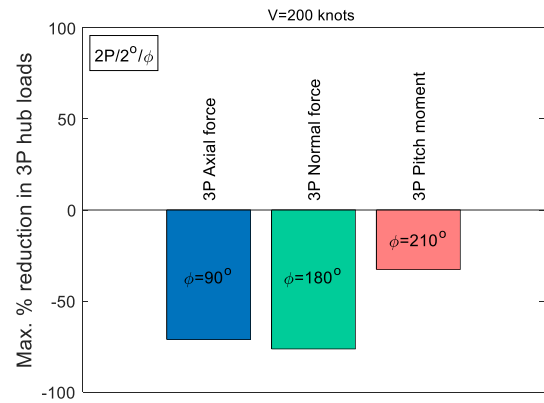
Figure 8. Maximum reduction in vibration index for various IBC conditions with a single harmonic input.



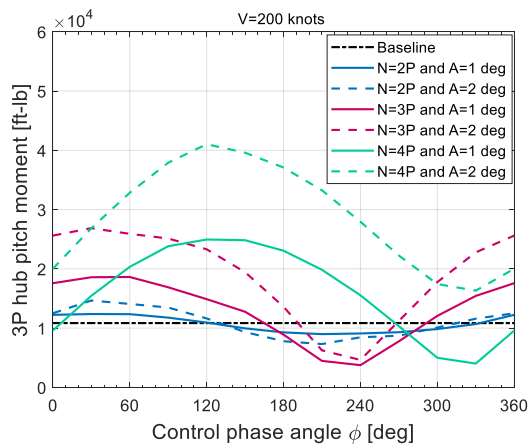
(a) Axial force



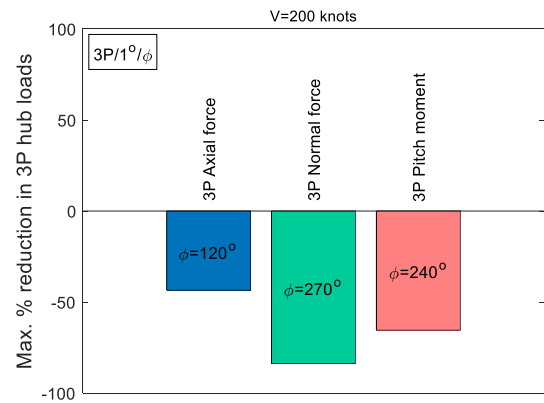
(b) Normal force



(b)  $2P/2^\circ/\phi$

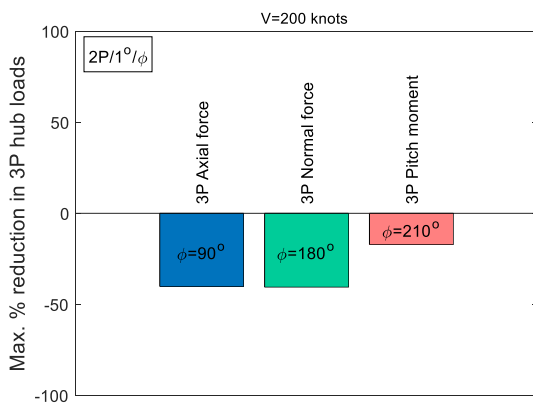


(c) Pitch moment

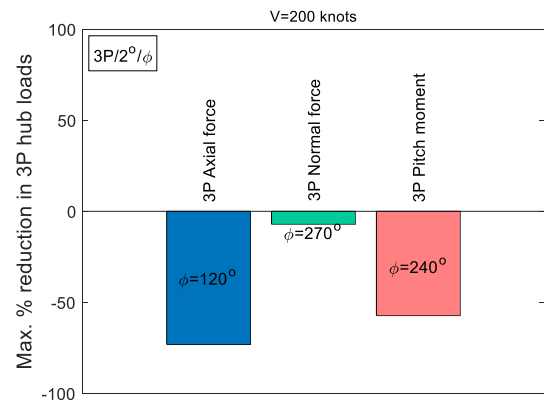


(c)  $3P/1^\circ/\phi$

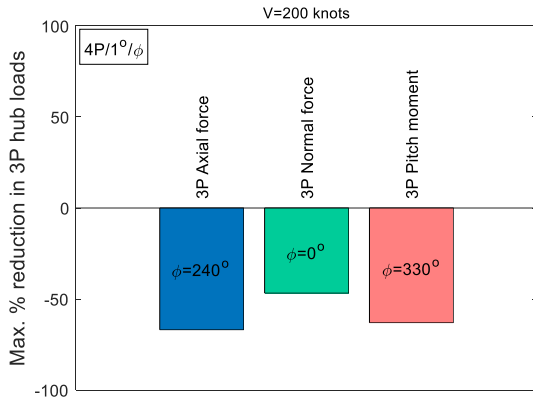
Figure 9. 3/rev hub load components in terms of control phase angle of IBC using a single harmonic input.



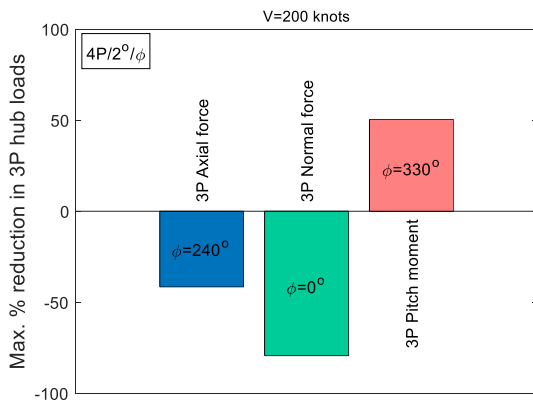
(a)  $2P/1^\circ/\phi$



(d)  $3P/2^\circ/\phi$



(e)  $4P/1^\circ/\phi$



(f)  $4P/2^\circ/\phi$

Figure 10. IBC input conditions with a single harmonic input for maximum reduction in 3/rev hub load components.

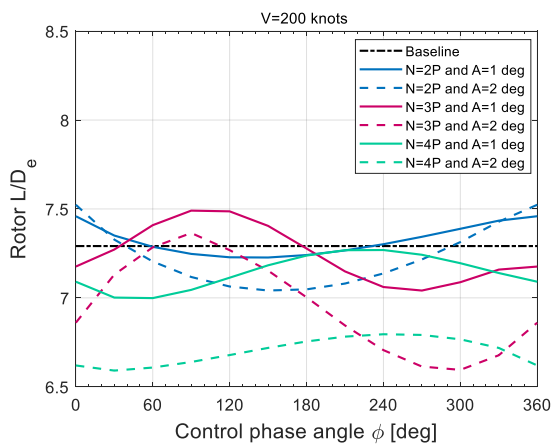


Figure 11. Rotor effective lift-to-drag ratio in terms of control phase angle of IBC using a single harmonic input.

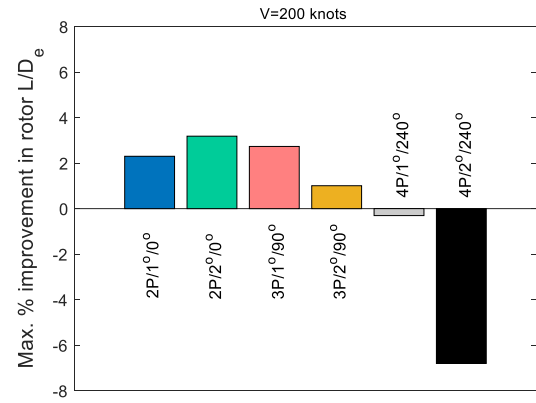


Figure 12. Maximum improvement in rotor effective lift-to-drag ratio for various IBC conditions with a single harmonic input.

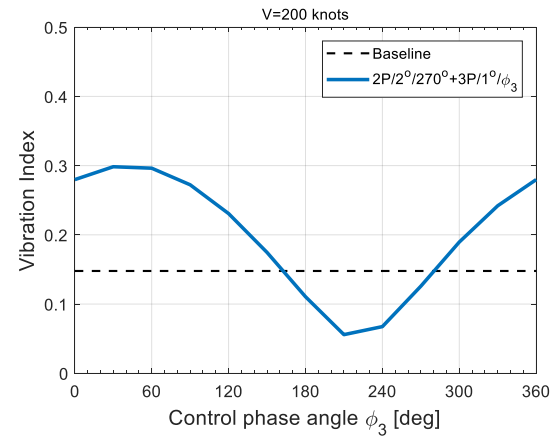
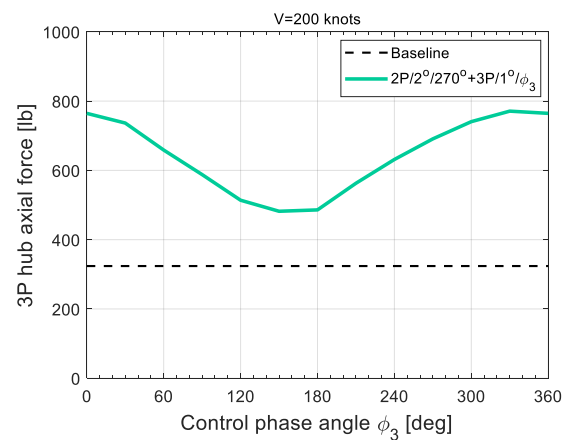
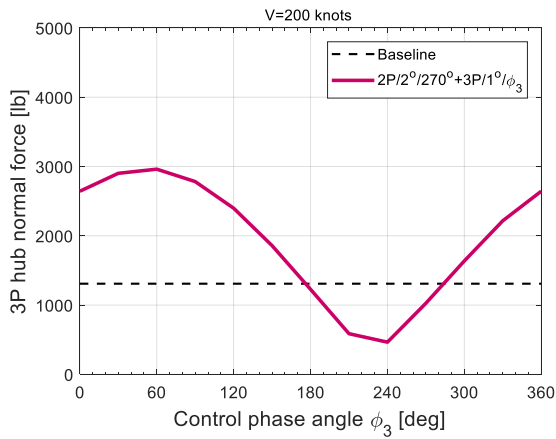


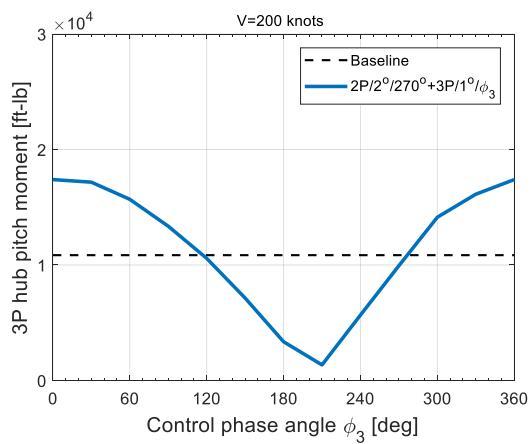
Figure 13. Vibration index in terms of control phase angle of IBC using multiple harmonic inputs.



(a) Axial force



(b) Normal force



(c) Pitch moment

Figure 14. 3/rev hub load components in terms of control phase angle of IBC using multiple harmonic inputs.

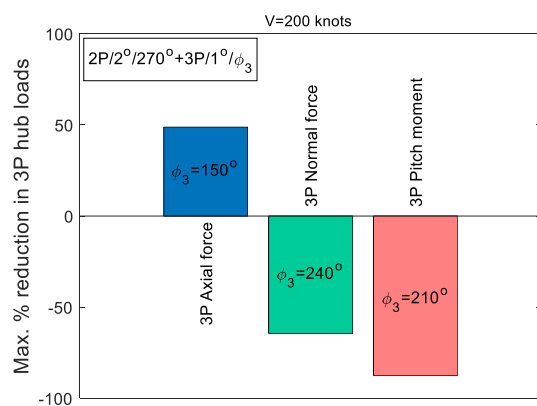


Figure 15. IBC input conditions with multiple harmonic inputs for maximum reduction in 3/rev hub load components.

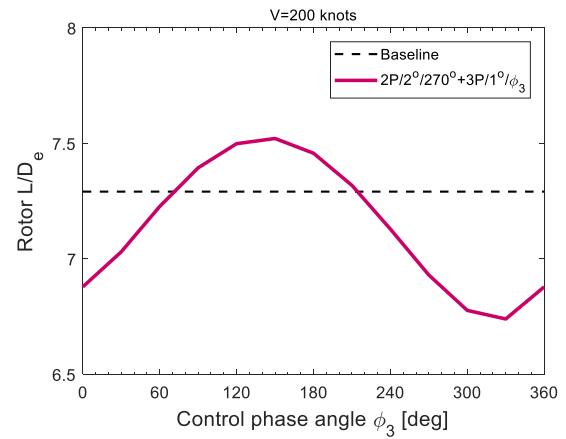


Figure 16. Rotor effective lift-to-drag ratio in terms of control phase angle of IBC using multiple harmonic inputs.

Table 1. Properties of XH-59A helicopter.

Hub type	Hingeless rotor
Radius, R [ft]	18
Number of rotors	2
Number of blades	3
Total solidity, $\sigma$	0.127
Tip speed [ft/sec]	
Pure helicopter	650
Compound helicopter	450
Maximum speed [knots]	
Pure helicopter	160
Compound helicopter	240
Horizontal tail	
Area [ft <sup>2</sup> ]	60
Span [ft]	15.50
Tail length [ft]	20.30
Vertical tail	
Area [ft <sup>2</sup> ]	30
Span [ft]	12
Tail length [ft]	20.30
Fuselage	
Length [ft]	40.5
Rotor separation [ft]	2.5
Power plants	
Lift	PT6T-3 turboshaft engine
Thrust	J60-P-3A turbojet engine

Table 2. Changes in vibration and rotor performance using IBC with multiple harmonic inputs.

Control phase angle ( $\varphi_3$ )	Percent change in	
	VI	L/D <sub>e</sub>
190°	-37.53	1.64
195°	-43.71	1.33
200°	-50.00	1.01